

9th Class 2016

Math (Science)	Group-I	Paper-I
Time: 20 Minutes	(Objective Type)	Max Marks: 15

Note: Four possible answers A, B, C and D to each question are given. The choice which you think is correct, fill that circle in front of that question with Marker or Pen ink in the answer-book. Cutting or filling two or more circles will result in zero mark in that question.

- 1-1- What should be added to complete the square of $x^4 + 64$:
- (a) $8x^2$ (b) $-8x^2$
(c) $16x^2 \checkmark$ (d) $4x^2$
- 2- Which order pair satisfy the equation $y = 2x$:
- (a) $(1, 2) \checkmark$ (b) $(2, 1)$
(c) $(2, 2)$ (d) $(1, 1)$
- 3- In a parallelogram, opposite sides are ---- .
- (a) Parallel \checkmark (b) Concurrent
(c) Congruent (d) None of these
- 4- The medians of a triangle cut each other in the ratio ---- .
- (a) $4 : 1$ (b) $3 : 1$
(c) $2 : 1 \checkmark$ (d) $1 : 1$
- 5- The right bisectors of the sides of a triangle are ----.
- (a) Congruent (b) Concurrent \checkmark
(c) Parallel (d) None of these
- 6- Imaginary part of $-i(3i + 2)$ is ---- .
- (a) $-2 \checkmark$ (b) 2
(c) 3 (d) -3
- 7- $\log e = \dots$, where $e \approx 2.718$.
- (a) 0 (b) 1
(c) $0.4343 \checkmark$ (d) ∞

- 8- Factors of $3x^2 - x - 2$ are ---- .
(a) $(x + 1)(3x - 2)$ (b) $(x + 1)(3x + 2)$
(c) $(x - 1)(3x - 2)$ (d) $(x - 1)(3x + 2)$ ✓
- 9- Distance between the points $(1, 0)$ and $(0, 1)$ is:
(a) 0 (b) $\sqrt{2}$ ✓
(c) 1 (d) 2
- 10- Unit of ratio is ---- .
(a) Second (b) Meter
(c) Kilogram (d) No unit ✓
- 11- The symbol used for "line" :
(a) \overline{AB} (b) $|AB|$
(c) \overleftrightarrow{AB} ✓ (d) \vec{AB}
- 12- Write $\sqrt[7]{x}$ in exponential form:
(a) $x^{1/7}$ ✓ (b) x
(c) x^7 (d) $x^{7/2}$
- 13- A triangle ---- is the union of a triangle and its interior.
(a) Region ✓ (b) Interior
(c) Exterior (d) Area
- 14- $(3 + \sqrt{2})(3 - \sqrt{2})$ is equal to:
(a) 7 ✓ (b) -7
(c) -1 (d) 1
- 15- $x = \text{----}$ is a solution of the inequality $-2 < x < \frac{3}{2}$.
(a) -5 (b) 3
(c) $\frac{3}{2}$ (d) 0 ✓

9th Class 2016

Math (Science)

Group-I

Paper-I

Time: 2.10 Hours

(Subjective Type)

Max. Marks: 60

(Part-I)

2. Write short answers to any Six (6) questions: 12

(i) If $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$, verify that $A + B = B + A$.

Ans L.H.S

$$\begin{aligned} A + B &= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} \\ &= \begin{bmatrix} 1+1 & 2-1 & 3+1 \\ 2+2 & 3-2 & 1+2 \\ 1+3 & -1+1 & 0+3 \end{bmatrix} \\ &= \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} \end{aligned}$$

R.H.S

$$\begin{aligned} B + A &= \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} \\ &= \begin{bmatrix} 1+1 & -1+2 & 1+3 \\ 2+2 & -2+3 & 2+1 \\ 3+1 & 1-1 & 3+0 \end{bmatrix} \\ &= \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} \end{aligned}$$

L.H.S = R.H.S

(ii) If $B = \begin{bmatrix} 6 \\ 5 \end{bmatrix}$, $A = \begin{bmatrix} 3 & 0 \\ -1 & 2 \end{bmatrix}$, find AB .

Ans $AB = \begin{bmatrix} 3 & 0 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 6 \\ 5 \end{bmatrix}$

$$\begin{aligned}
 &= \begin{bmatrix} 3(6) + 0(5) \\ -1(6) + 2(5) \end{bmatrix} \\
 &= \begin{bmatrix} 18 + 0 \\ -6 + 10 \end{bmatrix} \\
 &= \begin{bmatrix} 18 \\ 4 \end{bmatrix}
 \end{aligned}$$

(iii) Simplify by using rule of exponent: $\left(\frac{8}{125}\right)^{-4/3}$.

Ans $\left(\frac{8}{125}\right)^{-4/3} = \frac{1}{\left(\frac{8}{125}\right)^{4/3}} = \left(\frac{125}{8}\right)^{4/3}$

$$\begin{aligned}
 &= \frac{(125)^{4/3}}{(8)^{4/3}} \\
 &= \frac{(5^3)^{4/3}}{(2^3)^{4/3}} \\
 &= \frac{5^{3 \times 4/3}}{2^{3 \times 4/3}} \\
 &= \frac{5^4}{2^4} \\
 &= \frac{625}{16}
 \end{aligned}$$

(iv) Simplify and write your answer in the form of $a + bi$:

$$bi : \frac{-2}{1+i}$$

Ans $\frac{-2}{1+i} = \frac{-2}{1+i} \times \frac{1-i}{1-i}$

$$\begin{aligned}
 &= \frac{-2(1-i)}{1-i^2} \\
 &= \frac{-2+2i}{1-(-1)} \\
 &= \frac{-2+2i}{2} \\
 &= \frac{-2}{2} + \frac{2i}{2}
 \end{aligned}$$

(v) Find the value of x : $\log_{81} 9 = x$.

Ans \Rightarrow

$$\begin{aligned} \log_{81} 9 &= x \\ 81^x &= 9 \\ (9^2)^x &= 9 \\ 9^{2x} &= 9^1 \\ 2x &= 1 \\ x &= \frac{1}{2} \end{aligned}$$

(vi) Express as a single logarithm:
 $\log x - 2 \log x + 3 \log (x + 1) - \log (x^2 - 1)$.

Ans

$$\begin{aligned} &\log x - 2 \log x + 3 \log (x + 1) - \log (x^2 - 1) \\ &= \log x - \log x^2 + \log (x + 1)^3 - \log (x^2 - 1) \\ &= \log \frac{x(x + 1)^3}{x^2(x^2 - 1)} = \log \frac{(x + 1)^3}{x(x + 1)(x - 1)} \\ &= \frac{\log (x + 1)^2}{x(x - 1)} \end{aligned}$$

(vii) Reduce the following rational expression to the lowest form:

$$\frac{x^2 - 4x + 4}{2x^2 - 8}$$

Ans

$$\begin{aligned} \frac{x^2 - 4x + 4}{2x^2 - 8} &= \frac{x^2 - 2x - 2x + 4}{2(x^2 - 4)} \\ &= \frac{x(x - 2) - 2(x - 2)}{2(x^2 - 2^2)} \\ &= \frac{(x - 2)(x - 2)}{2(x + 2)(x - 2)} \\ &= \frac{x - 2}{2(x + 2)} \end{aligned}$$

(viii) If $x = 4 - \sqrt{17}$, then find $\frac{1}{x}$.

Ans

$$\begin{aligned} x &= 4 - \sqrt{17} \\ \frac{1}{x} &= \frac{1}{4 - \sqrt{17}} \\ &= \frac{1}{4 - \sqrt{17}} \times \frac{4 + \sqrt{17}}{4 + \sqrt{17}} \end{aligned}$$

$$\begin{aligned}
 &= \frac{4 + \sqrt{17}}{(4)^2 - (\sqrt{17})^2} \\
 &= \frac{4 + \sqrt{17}}{16 - 17} \\
 &= \frac{4 + \sqrt{17}}{-1}
 \end{aligned}$$

$$\frac{1}{x} = -4 - \sqrt{17}$$

(ix) Factorize: $x^2 - y^2 - 4x - 2y + 3$.

Ans By adding and subtracting 1.

$$\begin{aligned}
 &x^2 - y^2 - 4x - 2y + 4 - 1 \\
 &= x^2 - 4x + 4 - y^2 - 2y - 1 \\
 &= (x - 2)^2 - (y^2 + 2y + 1) \\
 &= (x - 2)^2 - (y + 1)^2 \\
 &= (x - 2 + y + 1)(x - 2 - y - 1) \\
 &= (x + y - 1)(x - y - 3)
 \end{aligned}$$

3. Write short answers to any Six (6) questions: 12

(i) Find H.C.F. of the polynomials by factorization:

$$x^2 - 4, x^2 + 4x + 4, 2x^2 + x - 6.$$

Ans

$$\begin{aligned}
 x^2 - 4 &= (x)^2 - (2)^2 \\
 &= (x + 2)(x - 2)
 \end{aligned}$$

$$\begin{aligned}
 x^2 + 4x + 4 &= x^2 + 2x + 2x + 4 \\
 &= x(x + 2) + 2(x + 2) \\
 &= (x + 2)(x + 2)
 \end{aligned}$$

$$\begin{aligned}
 2x^2 + x - 6 &= 2x^2 + 4x - 3x - 6 \\
 &= 2x(x + 2) - 3(x + 2) \\
 &= (x + 2)(2x - 3)
 \end{aligned}$$

Hence H.C.F = $(x + 2)$

(ii) Solve: $\frac{3}{y-1} - 2 = \frac{3y}{y-1}, y \neq 1$.

Ans

$$\frac{3}{y-1} - 2 = \frac{3y}{y-1}$$

$$(y-1) \times \frac{3}{y-1} - 2(y-1) = (y-1) \times \frac{3y}{y-1}$$

$$3 - 2y + 2 = 3y$$

$$-2y + 5 = 3y$$

$$3y + 2y = 5$$

$$5y = 5$$

$$y = 1$$

(iii) Find the solution set of:

$$|2x + 3| = 11.$$

Ans

$$|2x + 3| = 11$$

$$2x + 3 = 11$$

$$2x = 11 - 3$$

$$2x = 8$$

$$x = 4$$

$$2x + 3 = -11$$

$$2x = -11 - 3$$

$$2x = -14$$

$$x = -7$$

(iv) Define Cartesian Plane.

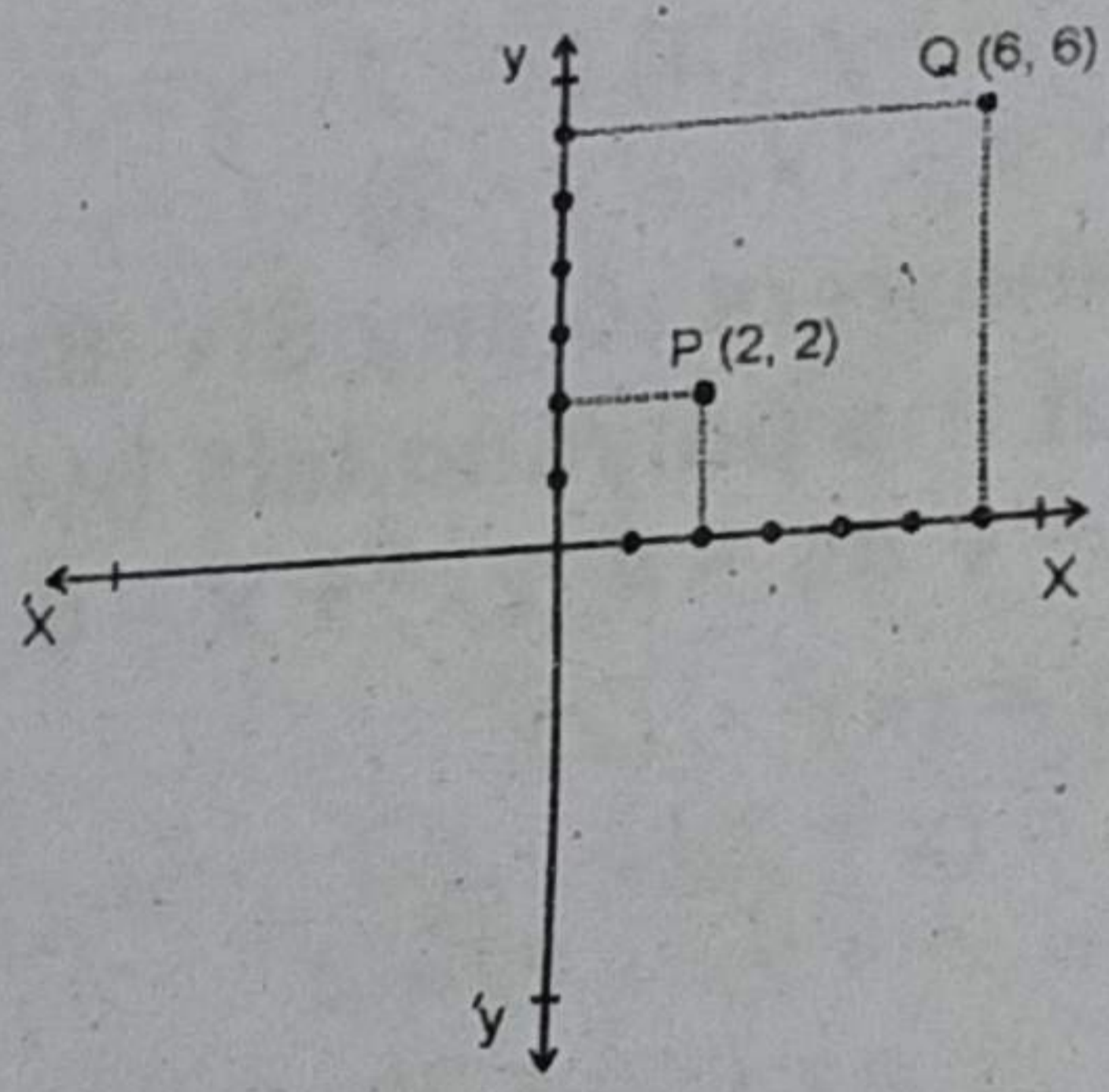
Ans

The Cartesian plane establishes (one-to-one) correspondence between the set of ordered pairs $R \times R = \{(x, y) | x, y \in R\}$ and the points of the Cartesian plane.

(v) Plot the points on quadrant:

P(2, 2), Q(6, 6)

Ans



(vi) Define scalene triangle.

Ans

A triangle is called a scalene triangle if measures of all the three sides are different.

(vii) Find the distance between the points: A(9, 2), B(7, 2).

Ans

$$|AB| = \sqrt{(7 - 9)^2 + (2 - 2)^2}$$

$$= \sqrt{(-2)^2 + 0}$$

$$= \sqrt{4}$$

$$|AB| = 2$$

(viii) What do you mean by SAS \cong SAS?

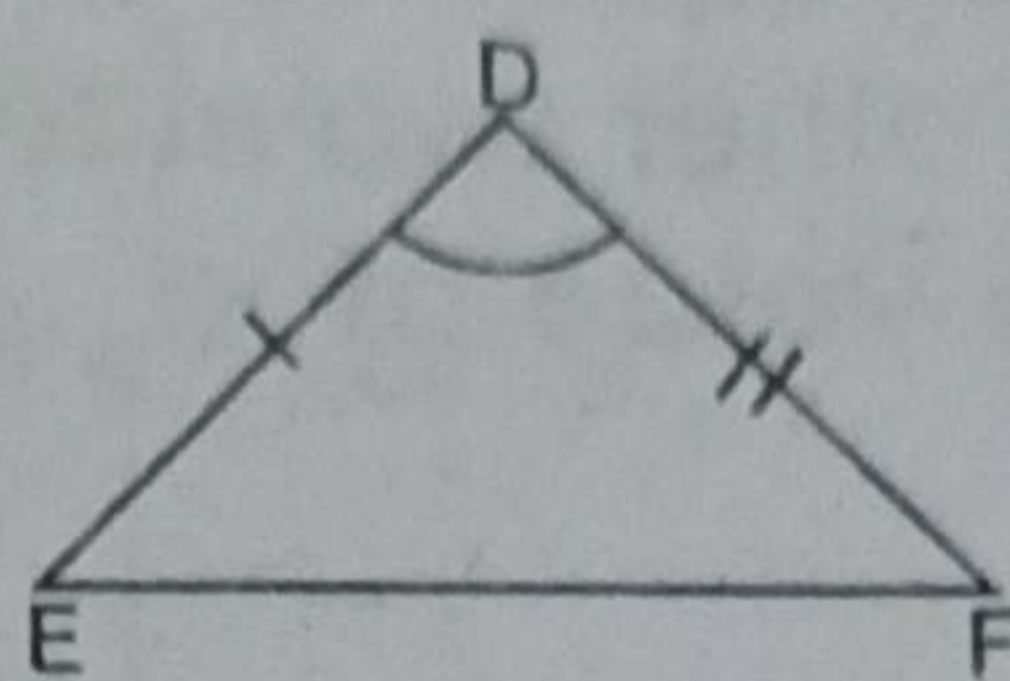
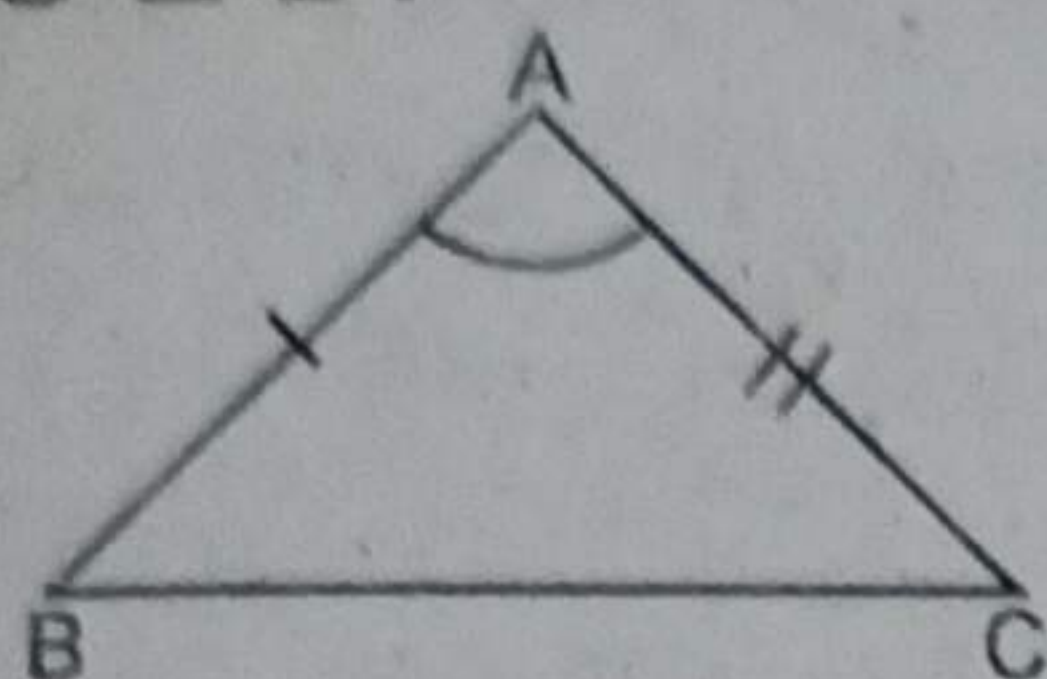
Ans

In any correspondence of two triangles, if two sides and their included angle of one triangle are congruent to

the corresponding two sides and their included angle of the other triangle, then the triangles are congruent.

In $\triangle ABC \leftrightarrow \triangle DEF$, shown in the following figures,

$$\text{if } \begin{cases} \overline{AB} \cong \overline{DE} \\ \angle A \cong \angle D \\ \overline{AC} \cong \overline{DF} \end{cases}$$



then $\triangle ABC \cong \triangle DEF$

(S.A.S Postulate)

(ix) Define parallelogram.

Ans A figure formed by four non-collinear points in the plane is called parallelogram. Its characteristics are as under:

1. Its equal opposite sides are of equal measure.
2. Its opposite sides are parallel.
3. Measure of none of the angle is 90° .

4. Write short answers to any Six (6) questions: 12

(i) Where do the right bisectors of the sides of an acute triangle and right triangle intersect each other?

Ans The right bisectors of the sides of an acute triangle intersect each other inside the triangle. The right bisectors of the sides of a right triangle intersect each other on the hypotenuse.

(ii) If 3 cm and 4 cm are lengths of two sides of a right angled triangle, then what should be the third side (hypotenuse) length of the triangle?

Ans

$$\begin{aligned} (\text{Hypotenuse})^2 &= (\text{Perpendicular})^2 + (\text{Base})^2 \\ (\text{Hypotenuse})^2 &= (3)^2 + (4)^2 \\ (\text{Hypotenuse})^2 &= 9 + 16 \\ (\text{Hypotenuse})^2 &= 25 \\ \sqrt{(\text{Hypotenuse})^2} &= \sqrt{25} \\ (\text{Hypotenuse}) &= 5 \text{ cm} \end{aligned}$$

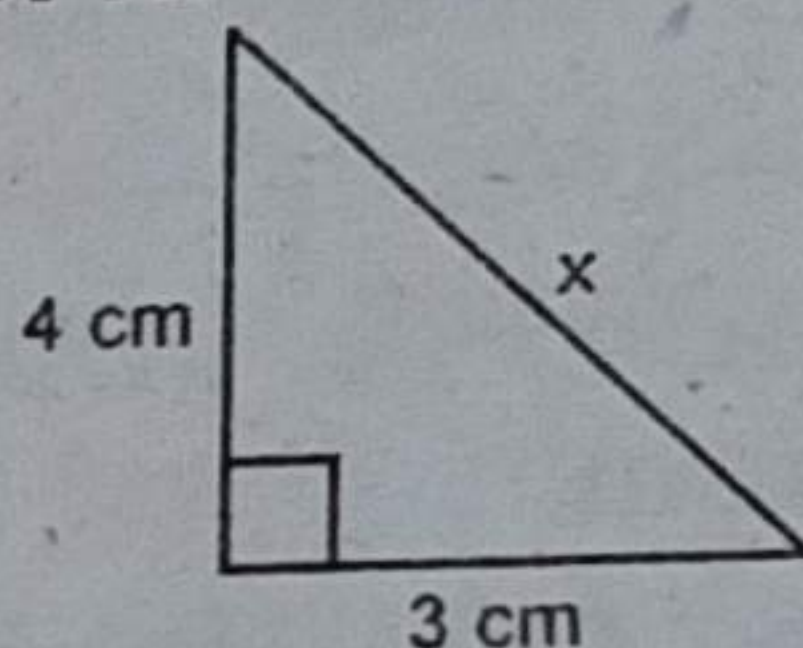
(iii) What is difference between a line and plane?

Ans For the sake of plane, two mutually perpendicular straight lines are drawn. But in that plane, we get a line after joining two points.

(iv) Define Pythagoras theorem.

Ans In a right angled triangle, the square of the length of hypotenuse is equal to the sum of the squares of the lengths of the other two sides.

(v) Find the value of x :



Ans (Hypotenuse)² = (Perpendicular)² + (Base)²
 $x^2 = 4^2 + 3^2$
 $x^2 = 16 + 9$
 $\sqrt{x^2} = \sqrt{25}$
 $x = 5 \text{ cm}$

(vi) Verify that following measures are the sides of right-angled triangle:

$$a = 5 \text{ cm}, b = 12 \text{ cm}, c = 13 \text{ cm}$$

Ans (Hypotenuse)² = (Perpendicular)² + (Base)²
 $(13)^2 = 5^2 + 12^2$
 $169 = 25 + 144$
 $169 = 169$

(vii) Define the rectangular region.

Ans A rectangular region is the union of a rectangle and its interior.

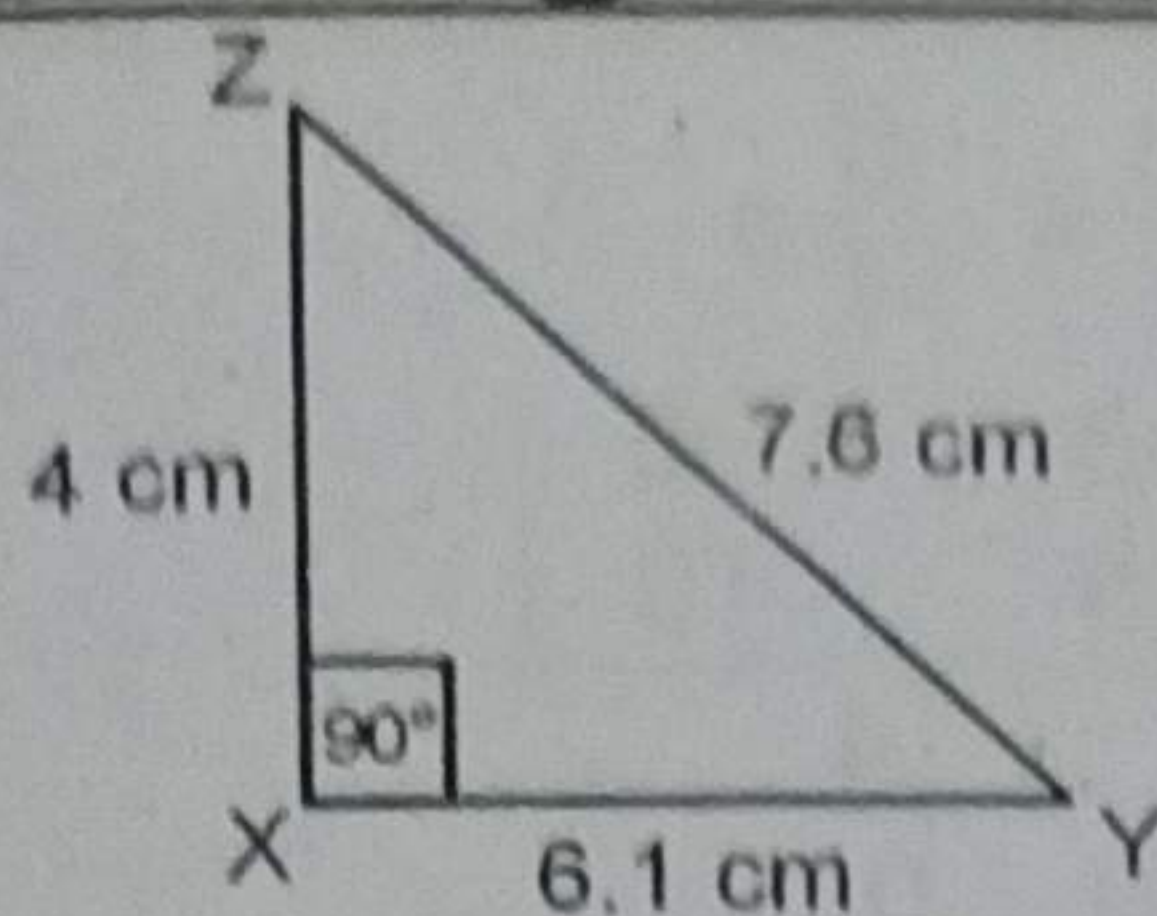
(viii) Define the incentre of a triangle.

Ans The internal bisectors of the angles of a triangle meet at a point called the incentre of the triangle.

(ix) Construct a triangle XYZ, in which:

$$m\angle X = 90^\circ, m\overline{XY} = 6.1 \text{ cm}, m\overline{YZ} = 7.6 \text{ cm}$$

Ans

**Constructive Procedure:**

1. Draw a line $XY = 6.1$ cm.
2. At point X, draw 90° angle.
3. At point Y, draw 7.6 cm long arc on Z.
4. Join Y and Z.
5. $\triangle XYZ$ is our required triangle.

(Part-II)

NOTE: Attempt Three (3) questions in all. But question No. 9 is Compulsory.

Q.5.(a) Solve the given system of linear equation by Cramer's rule:

$$3x - 2y = -6 \quad (4)$$

$$5x - 2y = -10$$

Ans

$$3x - 2y = -6$$

$$5x - 2y = -10$$

$$\begin{bmatrix} 3 & -2 \\ 5 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -6 \\ -10 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & -2 \\ 5 & -2 \end{bmatrix}$$

$$|A| = -6 + 10 = 4$$

$$A_x = \begin{bmatrix} -6 & -2 \\ -10 & -2 \end{bmatrix}$$

$$A_y = \begin{bmatrix} 3 & -6 \\ 5 & -10 \end{bmatrix}$$

$$x = \frac{|A_x|}{|A|} = \frac{\begin{vmatrix} -6 & -2 \\ -10 & -2 \end{vmatrix}}{4}$$

$$x = \frac{-6 \times (-2) - (-10 \times -2)}{4}$$

$$= \frac{12 - 20}{4} = -\frac{8}{4} = -2$$

$$y = \frac{|Ay|}{|A|} = \frac{\begin{vmatrix} 3 & -6 \\ 5 & -10 \end{vmatrix}}{4}$$

$$y = \frac{-30 + 30}{4} = \frac{0}{4} = 0$$

$$y = 0$$

(b) Use laws of exponents to simplify:

(4)

$$\frac{(81)^n \times 3^5 - (3)^{4n-1} (243)}{(9^{2n}) (3^3)}$$

Ans

$$\frac{(81)^n \times 3^5 - (3)^{4n-1} (243)}{(9^{2n}) (3^3)}$$

$$= \frac{(3^4)^n \times 3^5 - 3^{4n-1} \times 3^5}{(3^{2n})^2 \times 3^3}$$

$$= \frac{3^{4n+5} - 3^{4n-1+5}}{3^{4n} \times 3^3}$$

$$= \frac{3^{4n+5} - 3^{4n+4}}{3^{4n+3}}$$

$$= \frac{3^{4n+4} \times 3 - 3^{4n+4}}{3^{4n+3}}$$

$$= \frac{3^{4n+4} (3 - 1)}{3^{4n+3}}$$

$$= 3^{4n+4-4n-3} \times 2$$

$$= 3^1 \times 2$$

$$= 6$$

Q.6.(a) Use log tables to find the value of:

(4)

$$\frac{(1.23)(0.6975)}{(0.0075)(1278)}$$

Ans

$$x = \frac{(1.23)(0.6975)}{(0.0075)(1278)}$$

By taking log

$$\log x = \log 1.23 + \log 0.6975 - \log 0.0075 - \log 1278$$

$$\log x = 0.0899 + \bar{1}.8435 - \bar{3}.8751 - 3.1065$$

$$\log x = 0.0899 - 1 + .8435 + 3 - .8751 - 3.1065$$

$$= -1.0482$$

$$= -1.0482 - 2 + 2$$

$$\log x = \bar{2}.9518$$

Taking antilog

$$x = 0.0895$$

- (b) If $x^2 + y^2 + z^2 = 78$ and $xy + yz + zx = 59$, then find the value of $x + y + z$. (4)

Ans

$$\begin{aligned}(x + y + z)^2 &= x^2 + y^2 + z^2 + 2(xy + yz + zx) \\ &= 78 + 2(59) \\ &= 78 + 118 \\ &= 196\end{aligned}$$

$$(x + y + z)^2 = 14^2$$

Taking underroot both sides

$$\begin{aligned}\sqrt{(x + y + z)^2} &= \pm \sqrt{14^2} \\ x + y + z &= \pm 14\end{aligned}$$

Q.7.(a) Factorize: $64x^3 + 27y^3$ (4)

Ans

$$\begin{aligned}64x^3 + 27y^3 &= (4x)^3 + (3y)^3 \\ &= (4x + 3y)((4x)^2 + (3y)^2 - 4x \times 3y) \\ &= (4x + 3y)(16x^2 + 9y^2 - 12xy)\end{aligned}$$

- (b) For what value of k is $(x + 4)$ the H.C.F of $x^2 + x - (2k + 2)$ and $2x^2 + kx - 12$? (4)

Ans

$$2x^2 + kx - 12$$

$$P(x) = 2x^2 + kx - 12$$

$$\text{As } x + 4 = 0 \Rightarrow x = -4$$

$$\begin{aligned}P(-4) &= 2(-4)^2 + k \times (-4) - 12 \\ &= 32 - 4k - 12\end{aligned}$$

P must be zero

$$0 = 20 - 4k$$

$$20 = 4k$$

$$5 = \frac{20}{4} = k$$

$$q(x) = x^2 + x - 2k - 2$$

$$\begin{aligned}q(-4) &= (-4)^2 + (-4) - 2k - 2 \\ &= 16 - 4 - 2k - 2 \\ &= 10 - 2k\end{aligned}$$

R must be zero

$$10 = 2k$$

$$\frac{10}{2} = k$$

$$5 = k$$

Q.8.(a) Find the solution set of the equation: (4)

$$\frac{2}{3x+6} = \frac{1}{6} - \frac{1}{2x+4}, x \neq -2$$

$$\frac{2}{3x+6} = \frac{1}{6} - \frac{1}{2x+4}$$

$$\frac{2}{3x+6} + \frac{1}{2x+4} = \frac{1}{6}$$

$$\frac{2}{3(x+2)} + \frac{1}{2(x+2)} = \frac{1}{6}$$

$$\frac{4+3}{6(x+2)} = \frac{1}{6}$$

$$\frac{7}{6(x+2)} = \frac{1}{6}$$

$$6x + 12 = 42$$

$$6x = 42 - 12$$

$$6x = 30$$

$$x = \frac{30}{6}$$

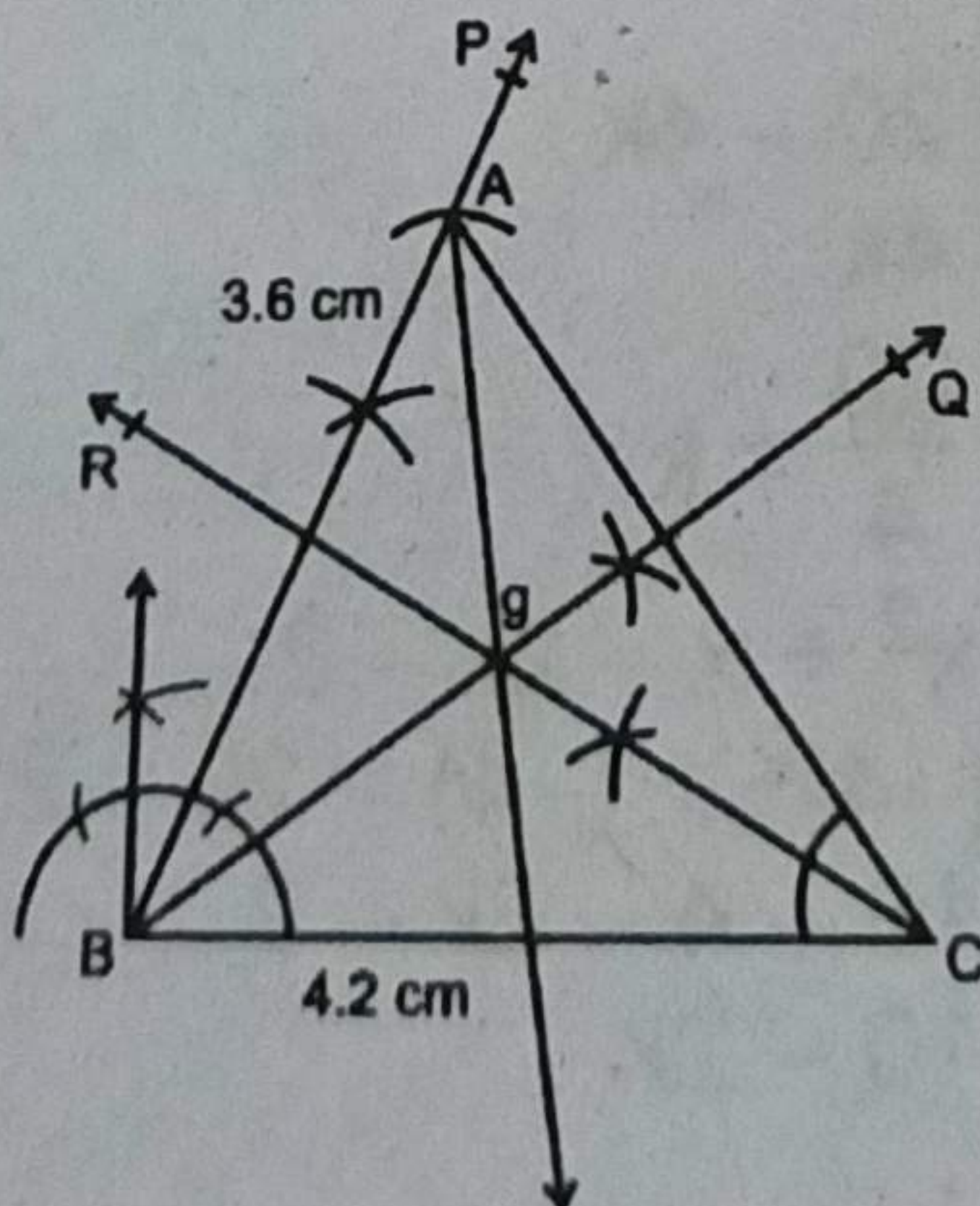
$$x = 5$$

{5}

(b) Construct $\triangle ABC$, draw the bisectors of its angles and verify their concurrency:

$m\overline{AB} = 3.6$ cm, $m\overline{BC} = 4.2$ cm and $m\angle B = 75^\circ$

Ans

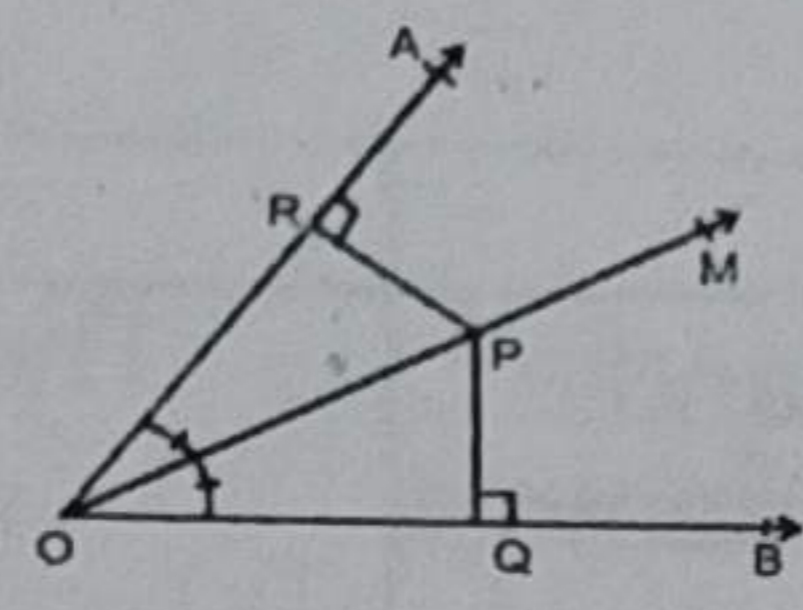


Constructive Procedure:

1. Take a line $\overline{BC} = 4.2$ cm.
2. Make an angle $\angle CBP = 75^\circ$.
3. Draw an arc of 3.6 cm at B which cuts \overrightarrow{BP} at A.
4. Join A and C.
5. ABC is the required triangle.
6. Take bisectors of angles as \overrightarrow{AP} , \overrightarrow{BQ} and \overrightarrow{CR} .

Q.9. Prove that any point on the bisector of an angle is equidistant from its arms. (4)

Ans



Given: A point P is on \overrightarrow{OM} , the bisector of $\angle AOB$.

To prove: $\overline{PQ} \cong \overline{PR}$ i.e., P is equidistant from \overrightarrow{OA} and \overrightarrow{OB} .

Construction: Draw $\overrightarrow{PR} \perp \overrightarrow{OA}$ and $\overrightarrow{PQ} \perp \overrightarrow{OB}$.

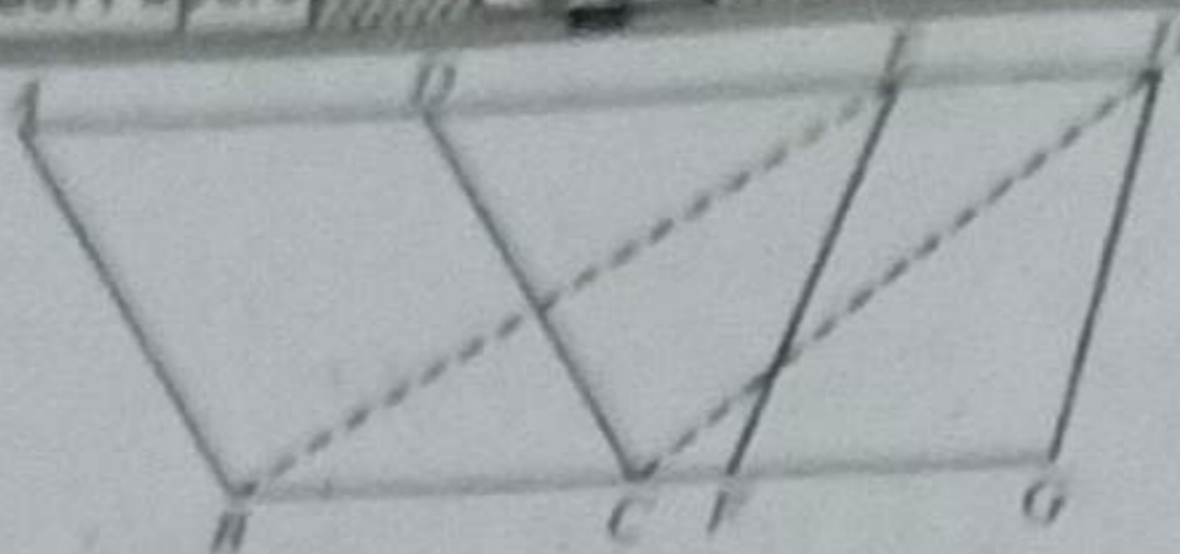
Proof:

Statements	Reasons
In $\triangle POQ \leftrightarrow \triangle POR$	
$\overline{OP} \cong \overline{OP}$	Common
$\angle PQO \cong \angle PRO$	Construction
$\angle POQ \cong \angle POR$	Given
$\triangle POQ \cong \triangle POR$	S.A.A \cong S.A.A
Hence $\overline{PQ} \cong \overline{PR}$	(corresponding sides of congruent triangles)

OR

Prove that parallelogram on equal bases and having the same (or equal) altitudes are equal in area.

Ans



- Given: Parallelogram ABCD, EFGH are on equal bases \overline{BC} and \overline{FG} , having equal altitudes.
- To prove: Area of (parallelogram ABCD) = Area of (\parallel^{gm} EFGH).
- Construction: Place the parallelograms ABCD and EFGH so that their equal bases \overline{BC} , \overline{FG} are in the straight line BCFG. Join \overline{BE} and \overline{CH} .

Proof:

Statements	Reasons
The given \parallel^{gm} ABCD and EFGH are between the same parallels. Hence ADEH is straight line \parallel to \overline{BC} $m\overline{BC} = m\overline{FG}$ $= m\overline{EH}$	Their altitudes are equal. (Given)
Now $m\overline{BC} = m\overline{EH}$ and they are parallel.	Given
\overline{BE} and \overline{CH} are both equal and parallel. Hence, EBCH is a parallelogram.	EFGH is a parallelogram.
Now \parallel^{gm} ABCD = \parallel^{gm} EBCH (i)	A quadrilateral with two opposite sides congruent and parallel is a parallelogram.
But \parallel^{gm} EBCH = \parallel^{gm} EFGH (ii)	Being on the same base \overline{BC} and between the same parallels.
Hence, area (\parallel^{gm} ABCD) = Area (\parallel^{gm} EFGH)	Being on the same base \overline{EH} and between the same parallels. From (i) and (ii)